

## A hierarchical network-based algorithm for multi-scale watershed delineation

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### Abstract

Watershed delineation is a process for defining a land area that contributes surface water flow to a single outlet point. It is a commonly used in water resources analysis to define the domain in which hydrologic process calculations are applied. There has been a growing effort over the past decade to improve surface elevation measurements in the U.S., which has had a significant impact on the accuracy of hydrologic calculations. Traditional watershed processing on these elevation rasters, however, becomes more burdensome as data resolution increases. As a result, processing of these datasets can be troublesome on standard desktop computers. This challenge has resulted in numerous works that aim to provide high performance computing solutions to large data, high resolution data, or both. This work proposes an efficient watershed delineation algorithm for use in desktop computing environments that leverages existing data, U.S. Geological Survey (USGS) National Hydrography Dataset Plus (NHD+), and open source software tools to construct watershed boundaries. This approach makes use of U.S. national-level hydrography data that has been precomputed using raster processing algorithms coupled with quality control routines. Our approach uses carefully arranged data and mathematical graph theory to traverse river networks and identify catchment boundaries. We demonstrate this new watershed delineation technique, compare its accuracy with traditional algorithms that derive watershed solely from digital elevation models, and then extend our approach to address subwatershed delineation. Our findings suggest that the open-source hierarchical network-based delineation procedure presented in the work is a promising approach to watershed delineation that can be used summarize publicly available datasets for hydrologic model input pre-processing. Through our analysis, we explore the benefits of reusing the NHD+ datasets for watershed delineation, and find that the our technique offers greater flexibility and extendability than traditional raster algorithms.

*Keywords:* Geographic Information Systems; Geographic Information Science; Terrain Analysis; Hydrologic Analysis; Spatial Analysis

## 1. Introduction

A watershed boundary defines the land surface that contributes streamflow to a single outlet location (Chow *et al.*, 1988). With advancements in geospatial software and readily available remotely sensed data, geographic information system (GIS) analysis have become widely used by hydrologists for determining a watershed boundary. Many research studies have investigated the various terrain processing components of GIS watershed delineation, such as methods for surface smoothing (Hutchinson, 1989), determination of flow direction (Douglas, 1986), slope and aspect calculations (Hodgson, 1998), depression filling (Jenson and Trautwein, 1987), and the extraction of drainage channels (O’Callaghan and Mark, 1984). These are only a few examples of the research that helped shape this domain; Moore *et al.* (2006) offers a more complete summary of the field.

The advent of high resolution digital terrain data and the need to analyze larger watersheds for environmental policy have resulted in efforts to advance the computational efficiency of terrain processing for hydrology applications. Recent studies have employed high performance computing (HPC) environments to overcome such computational limitations (Mineter, 2003; Wang and Armstrong, 2009; Huang *et al.*, 2011). Through these studies it has been demonstrated that HPC solutions have the potential for large performance gains by uncovering the intrinsic parallelism in traditional geospatial algorithms (e.g. Wang and Armstrong, 2009). Parallel algorithms operate by sharing the computational burden of data processing with multiple resources, and communicating data among each other using protocols such as the Message Passing Interface (MPI) (Xie, 2012). These approaches use advanced computational algorithms for delineating watersheds from digital elevation models (DEMs), mostly using the divide and conquer approach (Hutchinson *et al.*, 1996).

A similar, albeit fundamentally different approach for processing large datasets, is to leverage idle computing power by means of high throughput computing (HTC). HTC is a method for flexible distributed computing that takes advantage of relatively inexpensive collections of computing resources to achieve performance gains comparable to large HPCs (Thain *et al.*, 2005). It is a convenient solution for processing large amounts of data that enables organizations to take advantage of existing network compute power without the need for special computer hardware. The goal is to achieve speedup over longer periods of time using computing grids rather than emphasizing computer architecture (Chaudhry *et al.*, 2005). Recent studies have shown that this approach is effective in achieving significant computational speedup when processing large raster datasets (Gong and Xie, 2009; Huang and Yang, 2011).

While these approaches have been used extensively to processes large datasets, they require access to advanced computing techniques and resources. For instance, a great deal of expertise is required to design

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33 and use parallel HPC software modules because of their inherently high “learning curve,” which has a  
34 tendency to deter both commercial and academic developers (Mineter *et al.*, 2000; Lu *et al.*, 2010). An  
35 exception to this is are software that have adapted their algorithms to distribute computational load among  
36 processor threads to incorporate some of the HPC advantages (i.s. distributed computing) on desktop  
37 computers. TauDEM is one software application that employs this tactic to provide users with the best  
38 of both worlds (Wallis *et al.*, 2009). Similarly, HTC requires a large network of idle computers as well  
39 as specialized scheduling software to balance computing load across the network. Overall HPC and HTC  
40 solutions can be effective for data intensive computations, however they require specific computer hardware  
41 and a high level of sophistication. Moreover, many water resources professionals still rely on desktop  
42 computing environments as their main platform for watershed analysis. We lack a versatile approach of  
43 watershed delineation capable of efficiently resolving a wide range of spatial scales, without the use of HPC,  
44 HTC, or similar computing environments..

45 An alternative strategy for watershed delineation is to rely on pre-processed vector data. One example of  
46 this approach was presented by Djokic and Ye (2000), which aimed to overcome the computationally intensive  
47 nature of watershed delineation by separating static terrain-based properties from the delineation procedure.  
48 They proposed that since terrain measurements do not change often, they should not be linked directly to the  
49 delineation procedure. Rather, catchment geometries are processed prior to watershed delineation and later  
50 leveraged to construct a watershed boundaries. The major contribution of this work was their methodology,  
51 Fast Watershed Delineation (FWD), which is capable of rapidly yielding watershed boundaries using only  
52 desktop computing resources. Several additional efforts have been made to extend this technique for serving  
53 watershed delineations via web services. For example, the ArcGIS Watershed Delineation service provides a  
54 quick method for retrieving watershed delineations (Kopp *et al.*, 2013). Both of these approaches, however,  
55 require that computationally intensive catchment pre-processing routines have been completed prior to  
56 usage. Similar web based efforts have been made by the Environmental Protection Agency (EPA) and  
57 United States Geologic Survey (USGS) to produce the Navigation Delineation Service and StreamStats,  
58 respectively. The EPA Navigation Delineation Service leverages the NHD+ dataset to determine watershed  
59 boundaries and has been implemented by the Consortium of Universities for the Advancement of Hydrologic  
60 Science, Inc. (CUAHSI) HydroDesktop software, to delineate watershed boundaries which are then used to  
61 search for observation data within the Hydrologic Information System (Ames *et al.*, 2012). Similarly, the  
62 USGS StreamStats application offers a delineation service that is built using the NHD+ dataset and ArcGIS  
63 tools, but it also requires significant pre-processing (Guthrie *et al.*, 2009; Ries *et al.*, 2009).

64 Since the work of Djokic and Ye (2000), new datasets have become available such as the USGS National  
65 Hydrography Dataset Plus (NHD+). The NHD+ is a dataset derived from measured elevation, digitized  
66 hydrography, and the USGS Watershed Boundary Dataset (WBD) to accurately match known surface hy-  
67 drology. While the NHD+ contains elevation derived products such as flow direction and flow accumulation

68 grids for the entire U.S., it also provides pre-processed hydrologic catchment boundaries and river flow net-  
69 works. These can be leveraged to rapidly delineate watershed boundaries while eliminating data intensive  
70 pre-processing routines. Our approach is to leverage the concepts outlined by Djokic and Ye (2000), and the  
71 pre-processed NHD+ data to reconstruct watershed boundaries from pre-computed catchment geometries..  
72 Using graphing algorithms, upstream flow direction cells and ultimately catchment boundaries are identified  
73 for a given outlet location. We demonstrate how our approach is capable of rapidly yielding watershed  
74 boundaries for large areas on a desktop computer, while also delineating small catchments in a timely man-  
75 ner. It is then applied to the delineation of subwatersheds to demonstrate how it can be adapted for other  
76 common hydrologic tasks. Overall we demonstrate how our approach is a versatile solution for performing  
77 multi-scale watershed delineation on a desktop computer.

## 78 2. Method

79 Our method for watershed delineation is a two-step approach that borrows from graph theory to trans-  
80 form river flow attributes and known watershed surface runoff patterns into relational networks. While  
81 hydraulic river flows are used to identify fluxes between catchments, surface runoff is used to establish flow  
82 paths between raster cells. Furthermore, the hydraulic river flow graph is used to determine the “upper”  
83 portion of the watershed, and in contrast the surface runoff graph is used to determine the “lower” portion  
84 of the watershed. These upper and lower geometries are later combined to form the complete watershed  
85 boundary. This delineation technique requires both reach network and catchment input shapefiles, and  
86 relies on the specific relationships that can be established between them. More specifically, each feature in  
87 the reach network must have defined start and end nodes which are associated with other reaches in the  
88 network, as well as attributes that support network traversal. In addition, each reach must be associated  
89 with a single catchment geometry. This section explains how the NHD+ dataset can be leveraged to rapidly  
90 delineate watersheds, however as long as the aforementioned constraints are met the same technique can be  
91 applied to other datasets.

92 Our method uses graph theory to form relationships between the hydraulic characteristics of reaches as  
93 well as gravity driven flows among terrain grid cells. The basic concept is that a graph consist of independent  
94 entities (i.e. vertices) that are related to one another through connections (i.e. edges) (Marcus, 2008). This  
95 basic concept is illustrated in Figure 1. Once a graph is assembled, algorithms are used to navigate and  
96 traverse the nodes to solve a variety of problems, such as the famous traveling salesman problem (Hagberg  
97 *et al.*, 2008). There are also many different types of graphs, such as undirected, directed, multigraphs, etc.,  
98 which can be applied to solve problems in nearly every discipline (Rosen, 2003). In our work we use the  
99 NHD+ catchments to define graph vertices and the NHD+ reaches as graph edges between these nodes.  
100 The terrain is also represented as a graph, where the centroid of each cell in a DEM is a vertex and the flow

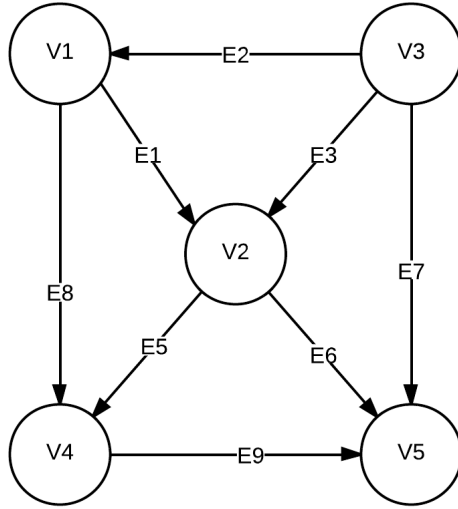


Figure 1: A basic directional graph consists of vertices that are connected by edges to describe the relationship among them.

101 direction at the node is used to establish an edge with its downstream neighbor. These two directed graphs  
 102 enable us to traverse the NHD+ dataset in a hydraulically upstream/downstream manner. Both of these  
 103 concepts are further explained in the following paragraphs.

104 First, consider that any given watershed may consist of one or more NHD+ catchments. Figure (2, i)  
 105 shows the NHD+ river network overlaying a small watershed consisting of pre-delineated catchments. These  
 106 catchments are related to one another by river flow attributes, for instance, each catchment drains into  
 107 exactly one of its neighbors. Since, each river in the NHD+ dataset is associated with an upstream and  
 108 downstream reach, this information can be used to create the graph illustrated in Figure (2, ii). This graph  
 109 network defines the water flow paths among catchments. Using our approach, we assume that a watershed  
 110 is encapsulated within this network and moreover consists of one or more catchments that can be identified  
 111 by hydraulic river flow attributes. In this manner, all catchments upstream of a given outlet location can be  
 112 quickly determined (Figure 2, iii), and subsequently merged together to resolve the geometry for the upper  
 113 portion of the watershed (Figure 2, iv).

114 A watershed outlet can be located anywhere within a catchment, not necessarily coinciding with the  
 115 drainage point used in the NHD+. Therefore, we must consider an alternative approach for resolving the  
 116 remaining, lower portion, of the watershed. This is accomplished by leveraging watershed surface flow  
 117 attributes. First, a mathematical graph is created using flow direction raster cell values. In a single-flow-  
 118 direction raster grid, each pixel contains a numeric value that defines the direction water flows from the

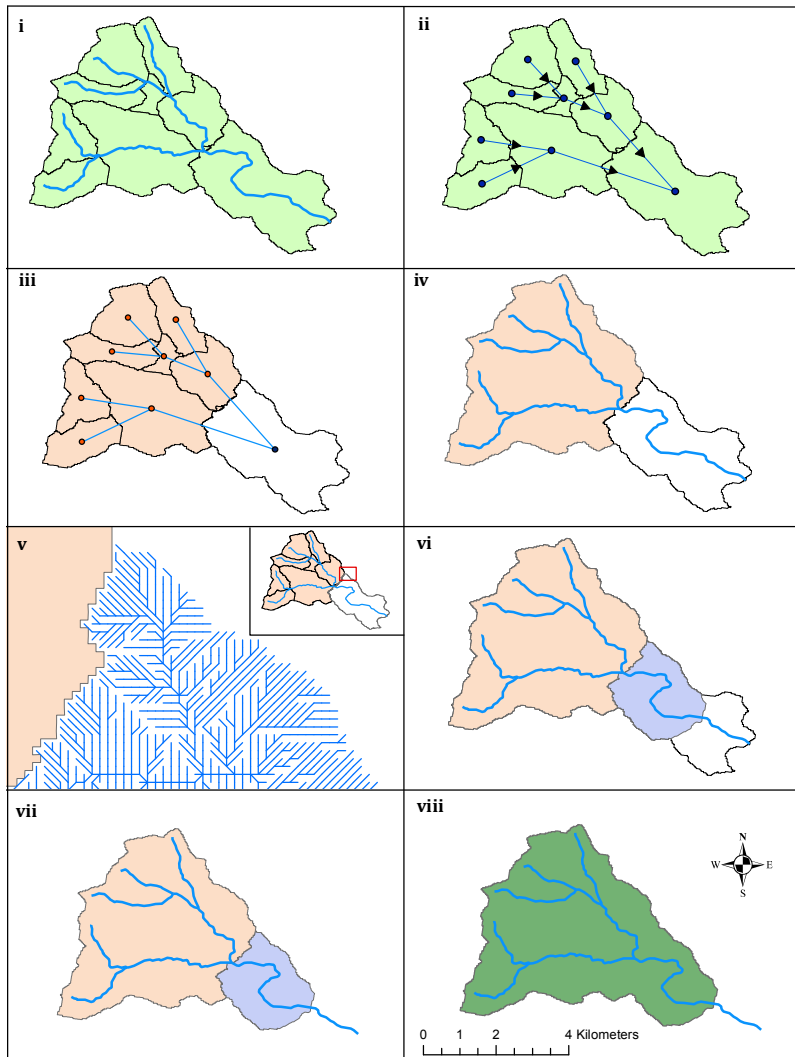


Figure 2: A graphical representation of the watershed delineation procedure.

119 surface in flooded conditions. By iterating through these cell values, a graph is constructed whereby each  
 120 node represents the centroid of a cell and each cell is connected to its “downstream” neighbor. Figure 2,  
 121 v) illustrates how an NHD+ catchment is transformed in to a dense graph network of cell-level flow paths.  
 122 Using graph theory, all of the raster cells contributing to a given location, i.e. watershed outlet, can be  
 123 determined by tracing the flow network in the upstream direction. This task is made trivial by leveraging  
 124 well-established software libraries that employ optimized graph traversing algorithms. Once the upstream  
 125 graph elements are known, the boundary for the lower geometry can be constructed by eliminating all  
 126 interior graph nodes (Figure 2, vi). Once the upper and lower portions of the watershed have been resolved  
 127 (Figure 2, vii), they are spatially merged together using GIS software to produce the complete watershed  
 128 boundary (Figure 2, viii).

129 To construct the catchment and flow direction graphs, existing software libraries can be leveraged such  
130 as the NetworkX Python library (Hagberg *et al.*, 2008). Using the aforementioned approach for constructing  
131 flow direction graphs, an edge is created between each cell and its “downstream” neighbor. However, applying  
132 this methodology for large areas results in extremely large graphs, and is therefore infeasible. For instance,  
133 creating a graph network consisting of 1 arcsecond data covering South Carolina, results in approximately  
134  $8.88 \times 10^7$  graph elements. A graph of this magnitude is impractical because its memory footprint is too large  
135 for most desktop computers. Since this graph is only used to resolve the lower portion of the watershed, it  
136 must only cover the area of an NHD+ catchment. Given this, single flow direction rasters can be extracted  
137 individually for each NHD+ catchment and graphs can be subsequently created. Moreover, these catchment  
138 level graphs can be serialized and stored for later use to further eliminate redundant operations. This  
139 technique results in one graph for each NHD+ catchment boundary. In contrast, the catchment graph is  
140 much less dense and as a result a single graph will suffice for an area covering South Carolina. By using this  
141 graphical approach, (1) all upstream catchments are identified, (2) the raster cells contributing flow to the  
142 outlet can be determined, and finally (3) the results of these operations can be merged to form a complete  
143 watershed.

144 This method can also be extended to support the delineation of subwatersheds, which is an important  
145 feature of GIS software for hydrology applications. Subwatersheds are generally derived from outlets that  
146 correspond with available observation data, and are often used to pre-process or summarize watershed related  
147 data for model inputs. A similar approach is taken to determine these subwatershed areas, albeit with a  
148 small modification. First all upstream catchments are determined. Next, the catchments corresponding to  
149 each individual outlet are isolated, such that each catchment is associated with only one outlet location. For  
150 each outlet, the upper catchments and lower catchment are combined in a manner consistent with Figure 2.

### 151 **3. Implementation**

152 The NHD+ provides many GIS data products to the public for free. The watershed delineation technique  
153 presented in this work uses several of these data products, as well as supplementary database files used to  
154 enhance their geospatial representations. While a newer version of the NHD+ dataset (version 2) is currently  
155 available, this work was initiated and completed using the NHD+ version 1. These data provide additional  
156 feature-based values and attributes to support the NHD+ vector data. This supplemental information  
157 can be leveraged to establish relationships between features of multiple NHD+ vector files. Moreover,  
158 the delineation algorithm relies on the NHD+ vector products and these additional datasets to establish  
159 relationships between digitized rivers and catchment boundaries to rapidly delineate watershed boundaries.

160 There exists a many-to-one relationship between the NHD+ river and catchment features. This means  
161 that there is at least one reach for every catchment defined in the dataset. As a result, the NHD+ reaches

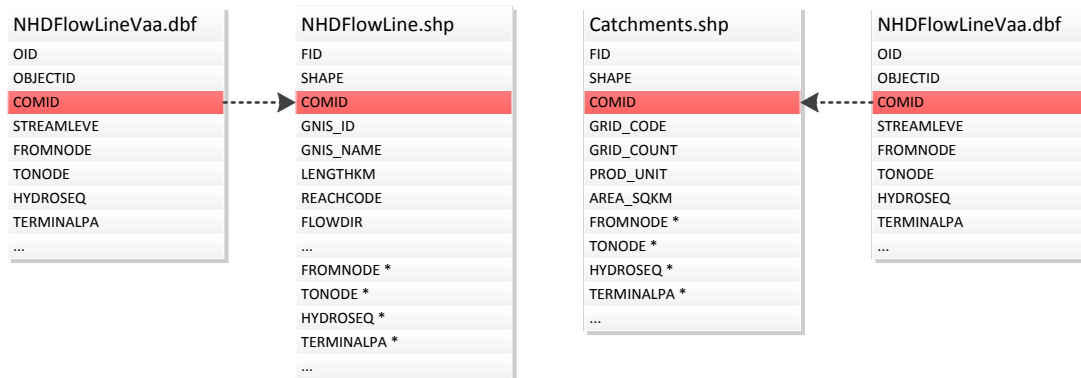


Figure 3: Joining the *NHDFlowLineVaa* dataset to both the *NHDFlowLines* and *Catchment* shapefiles provides the necessary attributes to form a connection between river reaches and catchments.

162 can be used to identify specific catchments, but to do this additional data attributes must be appended  
 163 to the reach dataset. Figure 3 illustrates how the *NHDFlowlineVAA.dbf* (i.e. Value Added Attributes,  
 164 VAA) data product can be used to enhance the *nhdflowline* and *catchment* vector files. By spatially joining  
 165 the VAA attributes to both of these datasets, additional information is appended to each feature such as  
 166 *fromnode*, *tonode*, *hydroseq*, and *terminalpa*. The *fromnode* and *tonode* attributes are unique identification  
 167 numbers that denote the start and end nodes for every reach in the dataset. The *hydroseq* parameter is a  
 168 unique hydrologic sequence number assigned to each reach in the dataset. These sequence identifiers are  
 169 assigned such that upstream reaches have larger values than downstream reaches. Finally, the *terminalpa*  
 170 parameter defines the hydrologic sequence number of the terminal feature of the reach network. This data  
 171 is used to create a directed graph which can then be used to identify upstream or downstream reaches from  
 172 any location within the network.

173 Using this upstream and downstream reach information, a graphical network is created to represent  
 174 relationships between digitized reaches, and ultimately the catchment features. First, NHD+ reach and  
 175 attribute data is transformed into a graphical network which later provides a mechanism for tracing flow  
 176 path's and identifying upstream reaches id's using graph tracing algorithms. Figure 4 illustrates how this  
 177 graph network is created using the Python programming language and the NetworkX library (Hagberg *et al.*,  
 178 2008). For each feature in the NHD+ reach network, a graph edge is established between its *fromnode* and  
 179 *tonode* identifiers. In addition, *hydroseq* and *terminalpa* values are stored as attributes on the graph object.  
 180 Once this process is complete for every reach feature, the graph is serialized for later use. Serialization is  
 181 an important part of this procedure because it enables the graph data object to be reloaded when needed,  
 182 rather than reconstructing it from scratch, which would be timely and inefficient. Using this graph, data for



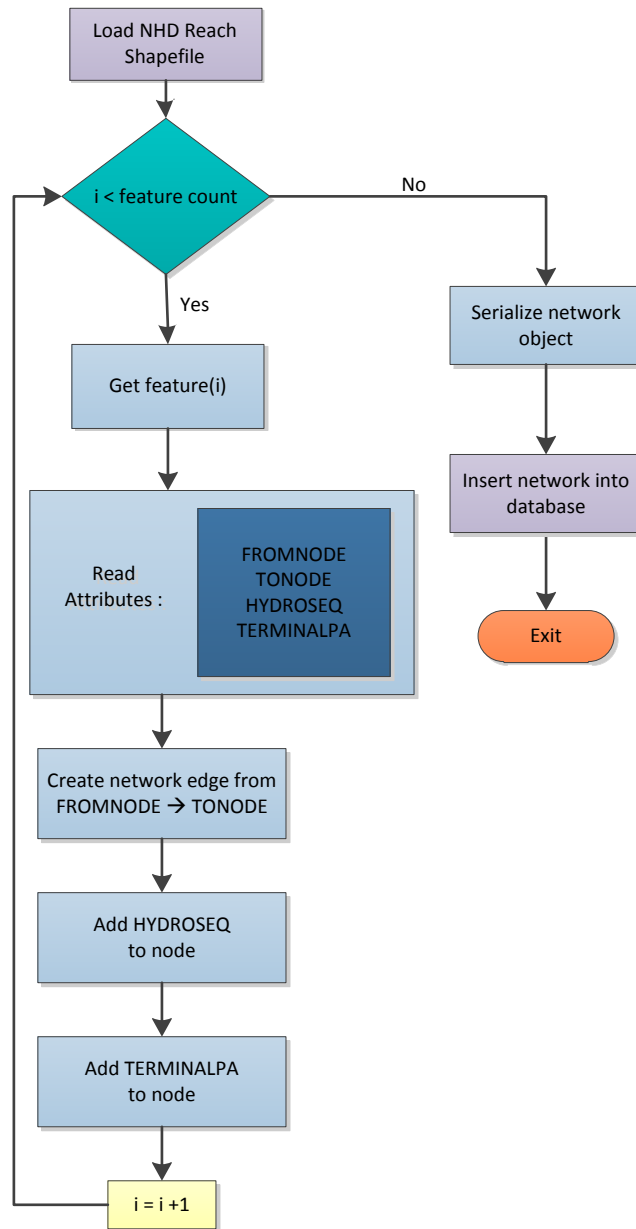


Figure 4: Flow chart illustrating how NHD+ digitized reaches are transformed into a mathematical graph network that is then serialized for later use.

183 all elements preceding a given node can be identified using NetworkX graph tracing functions. This provides  
184 an effective means for selecting the NHD+ reach elements that contribute flow to a common downstream  
185 location. For example, given a watershed outlet, all upstream reach attributes can be quickly identified.  
186 These data are then used to select the corresponding NHD+ catchment geometries.

187 Databases offer a mechanism for archiving large amounts of data in an easily accessible manner. Because  
188 of this, a database was chosen for storing the NHD+ catchment geometries and feature attributes. For  
189 this implementation the open source PostgreSQL database was chosen because it can easily be extended  
190 to support spatial data queries using PostGIS. This setup enables spatial data to be archived in an easily  
191 accessible format as well as retrieved using spatial data querying using standard SQL statements. Moreover,  
192 the PostGIS extension is equipped with numerous spatial operations that can be performed on-the-fly when  
193 querying data. Therefore, the NHD+ catchment geometry data was loaded into a PostgreSQL database  
194 along with the appended NHD+ value added attributes. In addition, an empty *network* database field  
195 was defined to store cell-level NetworkX graphs which are constructed on-the-fly using flow direction values  
196 within the selected catchment boundary. For instance, when an outlet is chosen and the corresponding  
197 catchment is identified, we must first check to see if a cell-level graph network exists in the database for this  
198 catchment. If not, it is created on-the-fly and saved in the database for later use. This design consideration  
199 aims to reduce unnecessary pre-processing steps, however this calculation can be performed ahead of time  
200 if maximum speed is a priority (e.g. web deployment). Once these catchment attributes are loaded into the  
201 database, spatial SQL queries are used to quickly extract catchment geometries when needed.

202 With the pre-processed NHD+ catchment data stored in a spatial database, features are queried using  
203 standard and spatial SQL statements. For instance, all catchments “upstream” of a graph location have  
204 a *hydroseq* identifier greater than that of the current location yet no greater than the largest *hydroseq*  
205 in the graph tree. The upper limit of this range is quantified as *maxseq*, and is calculated by simply  
206 iterating through all “upstream” nodes in the graph. Furthermore, all features must also belong to the same  
207 *terminalpa*. Therefore, given an outlet location as *outlet\_node*, all upstream catchments can be identified  
208 in a manner consistent with Figure 5. This results in the extraction of all NHD+ catchment geometries  
209 upstream of the outlet. These geometries are deserialized and subsequently merged together by performing  
210 a spatial union, which results in the upper portion of the watershed boundary. Since the watershed outlet  
211 can be located anywhere within the lowest catchment of the watershed, an alternative approach must be  
212 used to resolve the lower portion of the watershed boundary.

213 Since NHD+ catchment areas are relatively small in scale, mathematical graphs can be created to  
214 represent the flow paths between the interior flow direction values for each catchment. To create one of these  
215 networks, the NHD+ flow direction grid is first extracted over the area of a single catchment geometry. For  
216 each cell within this smaller grid, graph edges are created between each cell and its “downstream” neighbor.  
217 The “downstream” neighbor is easily identified for each cell using the single flow direction notation (i.e. D8

```

SELECT Geometry
FROM catchments_datatable
WHERE HYDROSEQ > outlet_node.HYDROSEQ
      AND HYDROSEQ <= MaxSEQ
      AND TERMINALPA == outlet_node.TERMINALPA

```

Figure 5: *SQL query for extracting catchment geometries stored in a PostgreSQL database using HYDROSEQ and TERMINALPA attributes.*

218 grid values). The final product is a graphical network consisting of edges that define the flow paths between  
 219 raster cells, which are confined to a single NHD+ catchment boundary (i.e. catchment flow path graph). As  
 220 mentioned earlier, this operation is performed on-the-fly when needed, and stored in the spatial database  
 221 within the *network* field as a serialized NetworkX object.

222 Using this flow direction graph, all nodes (i.e. cells) upstream of the outlet can be quickly identified using  
 223 graph traversing algorithms. The result is a set of coordinates that represent all cell locations “upstream”  
 224 of the outlet, but within the “most downstream” NHD+ catchment. By tracing the edge of this delineation  
 225 upstream from the outlet, the border locations can be identified. Once this boundary is identified, a polygon  
 226 object is created that represents the lower portion of the watershed. Finally, the upper and lower watershed  
 227 polygons are combined to form a single watershed boundary. Once complete, the overall catchment boundary  
 228 is saved as Well Known Text (WKT) and are later converted into Esri shapefile format for visualization.

#### 229 4. Application

230 Two studies were conducted to evaluate the application of the provided watershed delineation technique.  
 231 First it is evaluated in its ability to delineate watersheds at various spatial scales, then it is applied to the  
 232 delineation of subwatersheds. While similar Three community accepted software applications are used to  
 233 provide context for the general accuracy of the hierarchical algorithm. The first benchmark software, Esri’s  
 234 ArcGIS, is a widely used commercial-grade GIS suite. It consists of many tools for GIS analysis, including a  
 235 hydrology toolbox which is capable of performing a wide range of hydrology-related data processing routines.  
 236 In addition, ArcGIS contains a built-in Python interpreter, which enables these tools to be executed pro-  
 237 grammatically. This functionality was leveraged to automate the ArcGIS watershed delineation procedure,  
 238 which consisted of executing several tools in series.

239 The second benchmark software, Terrain Analysis Using Digital Elevation Models (TauDEM), is an open  
 240 source terrain analysis project (Tarboton *et al.*, 1997). It employs parallel computing concepts to divide large  
 241 datasets into smaller subsets. Terrain processing is performed on each of these subsets simultaneously, and  
 242 messages are passed between computational processes when necessary. Because of this design consideration,

243 it can theoretically perform terrain processing on very large datasets at a much faster rate than other  
244 software. It has been used in a number of academic studies from basic watershed analysis (Tarboton *et al.*,  
245 1997) to parallel terrain computations (Wallis *et al.*, 2009). Furthermore, the latest release of TauDEM  
246 (version 5.1) contains a toolbox plugin for ArcGIS (versions 9.3.1 – 10.0), therefore in a similar manner to  
247 ArcGIS, TauDEM tools can be executed autonomously through Python scripting. Our motivation for using  
248 these specific GIS software tools for comparison to our approach is to first provide context with regards to  
249 a closed-source commercially developed product, and then to an open-source academic tool.

250 The third benchmark software is ArcHydro Tools, which is a spatial processing tool pack that automates  
251 ArcGIS tools to perform advanced hydrology-related functions. In summary, it is an advanced information  
252 system that integrates the spatial and temporal aspects of hydrology to provide a complete GIS modeling  
253 and analysis suite (Maidment *ed.*, 2002). ArcHydro Tools is used in this work for its capacity to evaluate  
254 the accuracy and general efficiency of the provided delineation technique when applied to subwatershed  
255 delineation.

256 The testing all watershed delineations was performed using 32-bit Python interpreter on a desktop  
257 computer with a quad core 2.80 GHz processor having 4 GB of memory. The execution of the provided  
258 hierarchical delineation procedure is done by simply invoking the package from the commandline and passing  
259 it either one or multiple outlet point coordinates. The user must be careful to supply outlets in the spatial  
260 reference system that is used by the NHD+ catchment and river reach data. The algorithm uses several  
261 scientific libraries such as NumPY, GDAL, and NetworkX which must be installed separately. In addition,  
262 the NHD+ data must be downloaded, specifically the *catchments*, *river reaches*, and *supplementary* data  
263 files. Lastly, for this work data is stored in a PostgreSQL database using the PostGIS extension for handling  
264 spatial attributes.

#### 265 4.1. Multi-Scale Watershed Delineation

266 To evaluate our approach for various watershed scales, five basins were delineated along the South  
267 Carolina, Georgia border (i.e. the Savannah River basin) as well as one watershed that includes part of  
268 North Carolina (i.e. the Cooper River basin), shown in Figure 6. All watershed delineations were performed  
269 using input data provided by the NHD+ (i.e. flow accumulation and D8 flow direction), and the size of  
270 the datasets used in each scenario are summarized in Table 1. While the input data for each delineation  
271 scenario were provided at the same resolution, the grid sizes increased ascendingly in order to evaluate a  
272 wide range of computational scales. The experiments began with smaller headwaters and progressed to the  
273 larger downstream areas, concluding with the Savannah and Cooper River basins.

Table 1: *General properties of the input raster datasets used for each watershed delineation scenario.*

Dataset	Resolution	Dimensions	Grid Size	Disk Size
Scenario 1	30 m	926 × 891	$8.3 \times 10^5$	3.15 MB
Scenario 2	30 m	1835 × 2153	$39.5 \times 10^5$	15.07 MB
Scenario 3	30 m	5822 × 5848	$340.5 \times 10^5$	129.88 MB
Scenario 4	30 m	8287 × 7792	$645.7 \times 10^5$	246.32 MB
Scenario 5	30 m	10165 × 11011	$1119.3 \times 10^5$	426.97 MB

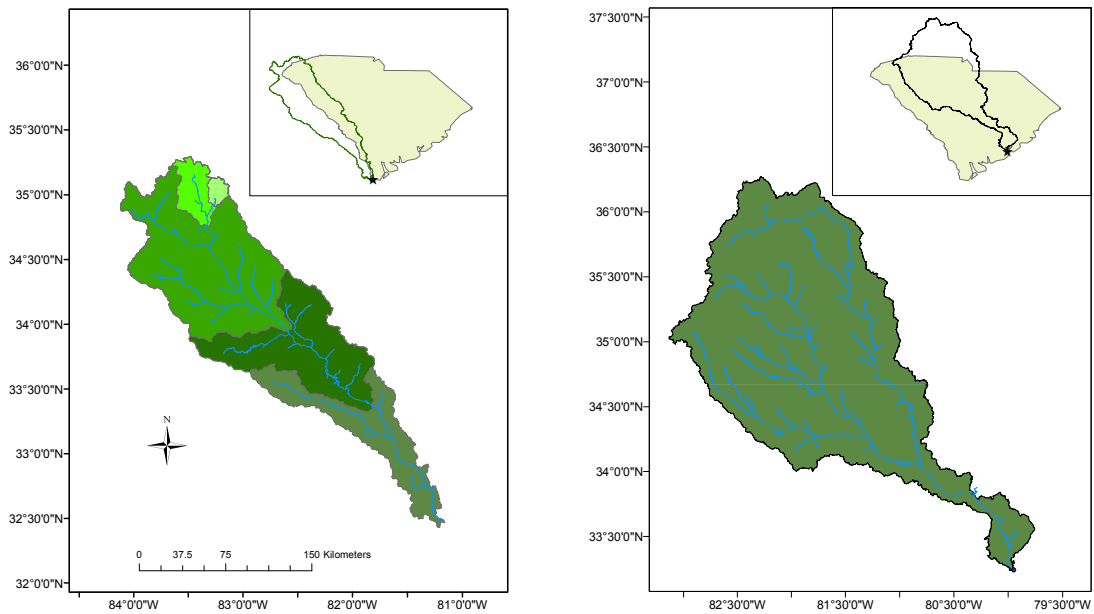


Figure 6: *Six watersheds were used to evaluate the performance of the hierarchical delineation approach. The Savannah River basin (Left) which was divided into five separate subwatersheds, and the Cooper River watershed (Right).*

274 The watershed delineation procedure using the ArcGIS software suite is illustrated in Figure 7. First, the  
 275 processing environment is prepared for executing ArcGIS tools. This consists of loading Python modules as  
 276 well as registering ArcGIS extensions. Once the environment has been prepared, the input raster grids (i.e.  
 277 flow direction and flow accumulation) are reduced to the extent of the known watershed boundary using the  
 278 ArcGIS Clip function. In practice this extent is often unknown, but since this experiment is evaluating the  
 279 speed of ArcGIS watershed delineation, we assume that ideal input information is available. Next, a new  
 280 point shapefile is created that contains a single feature, the watershed outlet location. This outlet point is  
 281 then relocated to the neighboring raster pixel that has the highest flow accumulation value, using the Snap  
 282 Pour Point tool. This is done to ensure that the outlet resides at a location of high flow accumulation,

283 as determined by the terrain topography. Once these steps are complete, the Watershed tool is executed.  
 284 Finally, the raster output from the watershed delineation is converted to a Esri polygon shapefile.

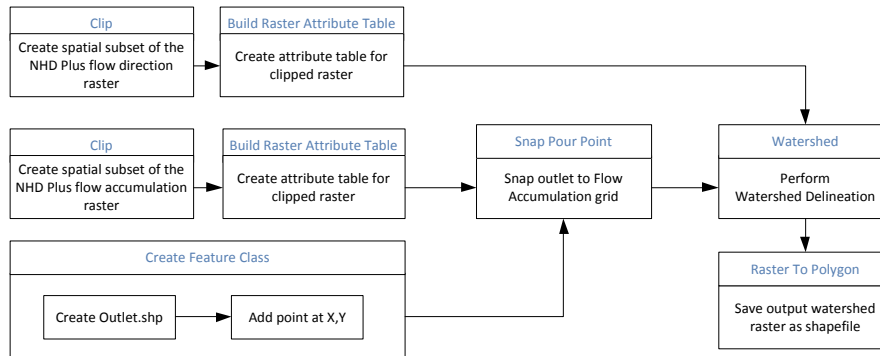


Figure 7: The procedure used for watershed delineation using ArcGIS tools, automated using the Python programming language.

285 TauDEM watershed delineation requires similar pre-processing routines to the ArcGIS approach. Many  
 286 of the data pre-processing steps use standard ArcGIS tools, for instance *Clip* and *Reclassify*, whereas the  
 287 actual watershed delineation uses only TauDEM tools which are indicated by the blue bold headings in  
 288 Figure 8. While ArcMap was used to prepare the input data for this watershed delineation, alternative  
 289 software could also be used for this task without affecting the results. Figure 8 follows the delineation  
 290 procedure that is suggested by Tarboton (2010). First, a new point feature is created containing the desired  
 291 outlet location of the watershed. Next, the NHD+ flow accumulation, elevation, and flow direction grids  
 292 are clipped to the approximate extent of the watershed. While this step is optional, it can have a significant  
 293 effect on the overall speed of the delineation by reducing the size of the input data. Map algebra is used to  
 294 select flow accumulation cells based on a user specified threshold which creates a new raster grid in which  
 295 rivers have a value of 1 and all other cells have a value of 0. This new river grid is then used to snap the  
 296 outlet onto the river network using the TauDEM *Move Outlets To Streams* tool. This aligns the desired  
 297 outlet with the watershed outlet as defined by the terrain. Next, the clipped flow direction grid is converted  
 298 from the tradition single-flow-direction notation, into the single-flow-direction values used by TauDEM (i.e.  
 299 {1,2,3,4,5,6,7,8}). The *Peucker Douglas Stream Definition* tool is executed using the snapped outlet, and the  
 300 clipped flow accumulation, flow direction, and elevation grids as input. The tool creates several new output  
 301 datasets that summarize various reach properties. One in particular, the stream raster grid, identifies all of  
 302 the reaches upstream of the outlet location. This grid is used as input to the *Stream Reach And Watershed*  
 303 tool, along with the snapped outlet, and clipped flow direction, flow accumulation, and elevation grids.  
 304 Execution of this tool results in several more raster grids such as stream order, stream connectivity, stream

305 coordinates, and a watershed grid. The watershed grid is supplied as input into the *Watershed Grid To*  
 306 *shapefile* tool which converts it into a vector file, thus completing the delineation procedure.

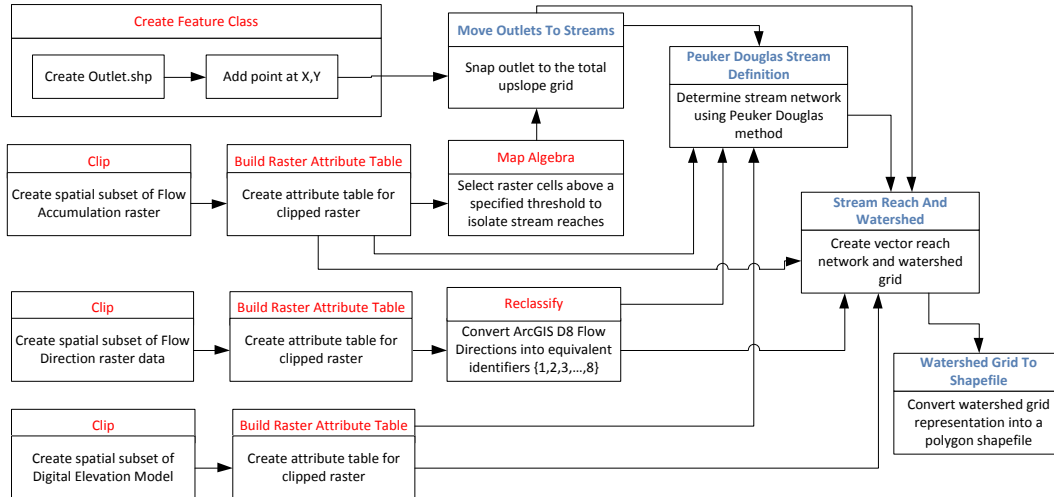


Figure 8: The procedure for watershed delineation using *TauDEM* tools, implemented using the *Python* programming language. The blue bold titles indicate operations performed by *ArcGIS* and bold titles indicate operations performed by *TauDEM*.

307 The provided approach and the two watershed processing techniques described above, were used to de-  
 308 lineate six different watersheds. The objective of this study is to first evaluate the accuracy of hierarchical  
 309 watershed delineation approach, and second to quantify its performance. Using the *ArcGIS* and *TauDEM*  
 310 processing routines as benchmarks, we evaluate how well our approach performs with respect to commer-  
 311 cial product and large scale terrain processing software. This experiment provides insight into the general  
 312 application of our watershed delineation approach compared with two widely used software suites. It re-  
 313 vealed that there exist differences in the watershed boundaries computed by each software suite. Table 2  
 314 illustrates these discrepancies for each scenario as the percent difference of the area taken with respect to  
 315 the average computed watershed area. This serves as a basis of reference for comparing the variations in  
 316 the watersheds computed by each algorithm. Minor boundary differences exist between the *TauDEM* and  
 317 *ArcGIS* calculations, however these were found to be a result of polygon simplification. In contrast, the  
 318 provided delineation exhibits larger variations with respect to the average computed watershed areas. These  
 319 discrepancies may be explained by the manner in which the *NHD+* dataset is created. For instance, the  
 320 *NHD+* is constructed using modified DEMs that closely match the known digitized hydrography as well  
 321 as the *WBD*. The catchment features used in our approach were modified to match river streamflow and  
 322 velocity estimates (Johnston *et al.*, 2009). In contrast, *ArcGIS* and *TauDEM* used surface elevation mea-

323 surements which were not modified in the same manner. We suggest that the boundary differences outlined  
 324 in Table 2 are a byproduct of the NHD+ design and are therefore inherent to our technique.

Dataset	Average Area km <sup>2</sup>	ArcGIS % difference	TauDEM % difference	Hierarchical % difference
Scenario 1	336.893	0.543	0.538	1.081
Scenario 2	1716.599	0.124	0.123	0.248
Scenario 3	13841.155	0.029	0.029	0.058
Scenario 4	21581.296	0.018	0.019	0.037
Scenario 5	26774.317	0.018	0.018	0.037

Table 2: *Differences in the watershed areas computed by each software suite. Variations are recorded relative to the mean watershed size for each scenario.*

325 To provide context for the efficiency of our approach we compared the overall computation time for  
 326 each of the delineation approaches. In this analysis we only interested in the time it takes for a user to  
 327 perform a delineation from start to finish. We found that ArcGIS performs exceptionally well at small  
 328 scales, however it follows a non-linear trend as the size of the dataset continues to grow. This is expected  
 329 because the ArcGIS tools that are used in this study are designed for general purpose desktop computing  
 330 and are not designed for processing very large data sets . In contrast, TauDEM which has the capability of  
 331 processing large raster data, executed the fastest for all watersheds delineations except the largest. Similar to  
 332 ArcGIS, it also scales in a non-linear fashion as dataset size increases. However, this work was all performed  
 333 on a computer using 4 processing threads and 4GB of memory. We expect that TauDEM will perform  
 334 more favorably on a high performance computer. Our technique is slower when delineating watersheds  
 335 at small scales, however it follows a linear trend as area increases, and completes the largest delineations  
 336 significantly faster than the other software systems. For instance, it finished approximately 2.1 times faster  
 337 than ArcGIS and 1.7 times faster than TauDEM for the Savannah River basin, and approximately 2.5 times  
 338 faster than ArcGIS and 2.7 times faster than TauDEM for the Cooper River basin. We believe that this  
 339 speedup is because our approach is able to leverage pre-processed catchments rather than directly processing  
 340 DEMs. This supports our argument that using pre-processed national datasets, such as the NHD+, has  
 341 some distinct advantages over DEM processing approaches. However, as the number of catchments increases  
 342 (i.e. dataset size increases), the amount of time dedicated to geometry extraction from the database and  
 343 geometry merging, becomes more pronounced. This insight suggests that future work should focus on the  
 344 internal algorithms used in our approach. These basic benchmarks are an average of several simulation  
 345 runs in which raster pre-processing routines have been omitted. Therefore, we can expect the end-to-end



346 execution times to increase with inclusion of raster data preparation, whereas this will not effect the our  
 347 approach.

#### 348 4.2. Subwatershed Delineation

349 Another important feature of GIS software for hydrology applications is the ability to delineate subwa-  
 350 tershed areas. Relatively little work is required to extend our approach to subwatershed delineation, which  
 351 further demonstrates its flexibility. The same general methodology is applied to determine watershed areas,  
 352 therefore only a small extension required to provide the additional functionality of deriving subwatershed  
 353 areas from NHD+ catchments.

354 The extension is largely made to perform the procedure outlined in Section 3 over a list of outlet points  
 355 rather than a single location. This is illustrated by the loop mechanism in Figure 9, in which the geometry  
 356 and graph networks are queried for each outlet provided by the user. The upper and lower watershed areas  
 357 are determined for each outlet by following the methodology presented in Section 3. However, once all the  
 358 upper catchments have been identified for all outlets, they are isolated such that each catchment geometry  
 359 can only belong to one subwatershed, which in turn, is associated with one outlet. This is done to eliminate  
 360 redundant merging of catchment geometries. This can also be done in a less efficient manner by first merging  
 361 the upper and lower geometries for each outlet and then subtracting them from one and other to derive the  
 362 subwatersheds. The subwatershed boundaries are used to create a polygon output file, and the outlet points  
 363 are used to create a point output file. Together, these new files summarize the subwatershed topographic  
 364 characteristics of a particular region.

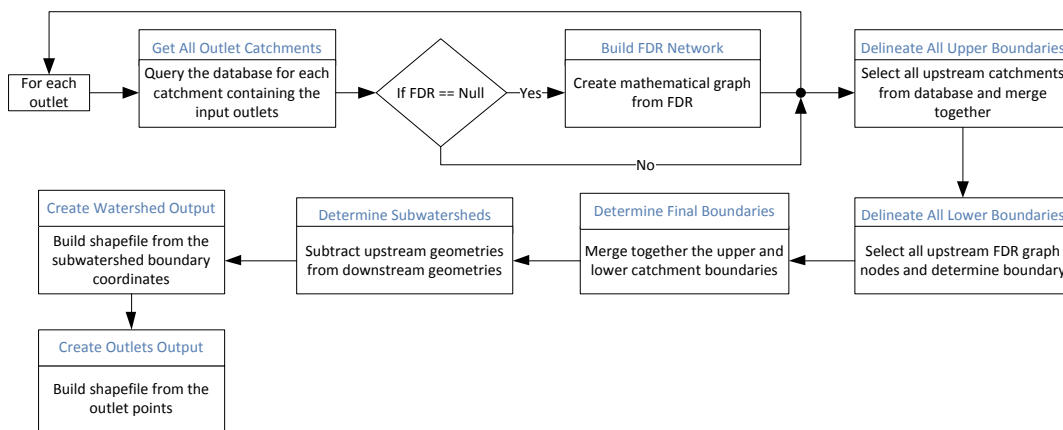


Figure 9: The procedure for subwatershed delineation using the hierarchical technique.

365 For comparison purposes, a widely used software suite is used to calculate the subwatersheds over the  
 366 same area: Arc Hydro Tools. While Arc Hydro Tools is capable of performing a myriad of advanced

367 hydrology-related processing, we only leverage its subwatershed delineation functionality, outlined in Figure  
 368 10. First, a point shapefile is created using a list NHD+ output locations. Five additional attribute fields  
 369 are created to match the format of the Arc Hydro Tools “Batch Point” file that is required as input to the  
 370 *Batch Subwatershed Delineation* tool. Next, values for these attribute fields must be assigned, specifically,  
 371 *BatchDone* is set to 0 and *SnapOn* is set to 1. These values indicate that (1) batch processing has not  
 372 been completed and (2) that each outlet must be snapped onto the river network. Once complete, these  
 373 points are imported into the Arc Hydro Tools geodatabase using ArcCatalog. Next, the river network is  
 374 defined using the *Stream Definition* tool. This tool creates a raster product derived from the NHD+ flow  
 375 accumulation grid that consists of cells having an accumulation greater than a user defined value. Finally,  
 376 the *Batch SubWatershed Delineation* tool is executed to delineate basins for each of the outlets provided.

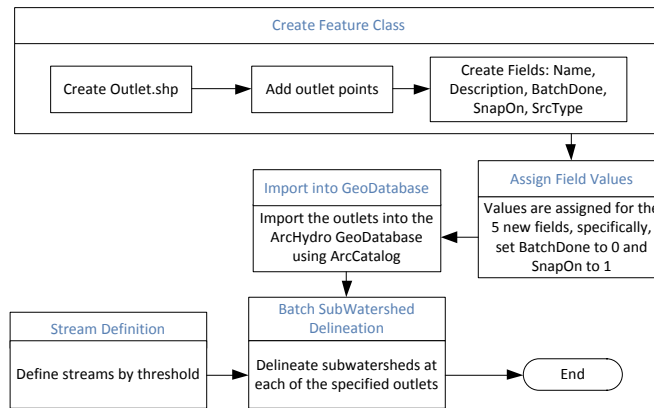


Figure 10: The procedure for subwatershed delineation within ArcGIS, using Arc Hydro Tools.

377 Both of these approaches were applied to delineate watersheds at 49 locations, corresponding to USGS  
 378 streamflow monitoring gages. Figure 11 shows the boundaries that were delineated using each of the afore-  
 379 mentioned GIS approaches. The hierarchal technique finishes this operation in 69 seconds, whereas using  
 380 Arc Hydro this took 2 minutes. Again, discrepancies exist between the boundary calculated by Arc Hydro  
 381 Tools using raster computations and the boundary that was assembled from NHD+ catchments using the  
 382 hierarchical approach. Insets (i) and (ii) of Figure 11 illustrate the nature of the boundary differences we  
 383 found. In both cases, small catchment areas are left out of our calculation which contradicts the boundary  
 384 calculated directly from the terrain elevation using raster calculations. As described in Section 4.1, we  
 385 believe that this is a direct result of how the NHD+ dataset was created and the flow attributes therein.  
 386 In the first inconsistency, NHD+ derived boundaries don't exactly match the those calculated using raster  
 387 computations. Upon further inspection it appears that this has been corrected in version 2 of the NHD+  
 388 dataset. The second case, however, is due to the river flow attributes that we used to trace upstream reaches  
 389 and subsequently catchments. This may be due to corrections that were made to the natural terrain to ac-

390 count for the actual hydrography of the surface, or they could mistakes within the NHD+ dataset that must  
391 be corrected.

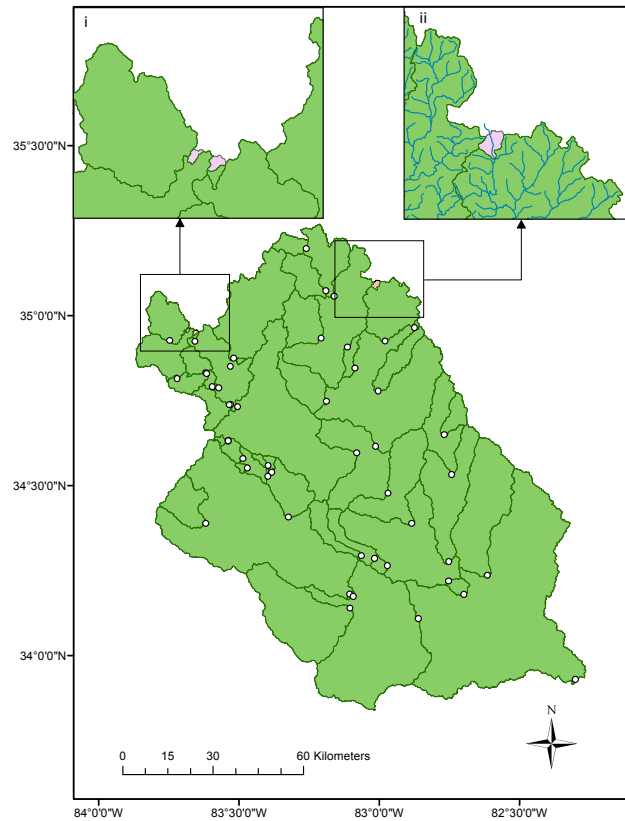


Figure 11: *Subbasins were delineated at USGS streamflow stations using Arc Hydro Tools and the hierarchical approach. Boundary differences were found when compared with raster-based delineation and are illustrated by the lighter catchments in insets (i) and (ii).*

## 392 5. Summary and Discussion

393 A watershed delineation technique was presented that uses existing GIS vector and raster data to re-  
394 solve watershed boundaries for a wide range of spatial scales. It leverages freely available input data and  
395 open-source software which makes it easily accessible to a wide range of hydrologic scientists. Traditional wa-  
396 tershed delineation approaches perform raster computations directly on DEM's, which inadvertently results  
397 in redundant computations (Djokic and Ye, 2000). Our approach is advantageous when large pre-delineated  
398 watershed datasets are available. When this is not the case, traditional DEM processing may be the pre-

399 ferred option. While these datasets can be created manually (Djokic and Ye, 2000), the encouragement of  
400 programs similar to the USGS NHD+ by international agencies, would enable our algorithm to be easily  
401 adopted for a wide range of hydrologic science applications. This approach will not replace traditional raster  
402 processing algorithms which, among numerous other applications, is instrumental to deriving raster data  
403 products required for model simulation (e.g. Quinnet *et al.*, 1995) . However, its versatility lends it useful as a  
404 hydrologic data processing tool that can be used to spatially summarize data attributes on a catchment or  
405 subcatchment level. It can also be used as a boundary for search, collection, and/or extraction of simulation  
406 input data (e.g. observation and spatial data) in a web based environment.

407 By leveraging pre-processed watershed catchment vectors, our technique offers an efficient solution to  
408 watershed delineation. Furthermore, the input data used to construct watershed boundaries is pre-processed  
409 by the USGS (i.e. NHD+), thus eliminating time intensive processing routines which have been necessary in  
410 past works (e.g. Djokic and Ye, 2000; Arge *et al.*, 2006; Danner *et al.*, 2007). In addition, the NHD+ dataset  
411 has been checked for accuracy by an interdisciplinary team of USGS and U.S. EPA scientists (Bondelid  
412 *et al.*, 2010). Moreover, the quality of watershed delineations should continue to improve with each release  
413 of the NHD+ dataset. For example implementing our method on the newest version of the NHD+ (version  
414 2) will automatically correct any errors that were detected in the previous version of the dataset. This is  
415 significant because it streamlines the process of upgrading surface data by eliminating the need to download  
416 numerous individual elevation raster grids which not only saves time, but also storage space.

417 Our approach for watershed delineation uses NHD+ data products to rapidly assemble watershed bound-  
418 aries. First, a small portion of the watershed is determined by tracing the grid cells upstream of the outlet  
419 location. This upstream trace identifies all cells that contribute flow to the outlet, but that are limited to  
420 the NHD+ catchment in which the outlet resides. This was made possible by borrowing from mathematical  
421 graph theory and leveraging the NetworkX graphing library (Hagberg *et al.*, 2008). The upper portion of the  
422 watershed is determined using the flow relationships between the NHD+ digitized river reaches to identify all  
423 upstream rivers and their respective catchments. The geometries for these catchments are then merged and  
424 later combined with the lower portion of the watershed to complete the delineation. Because this technique  
425 does not require grid processing, it can rapidly resolve a watershed boundary with a little computational  
426 overhead. Furthermore, it was shown that our algorithm is advantageous for delineating watersheds at a  
427 wide range of scales as well as delineating subwatersheds.

428 The application of our delineation approach demonstrates a method for delineating watersheds and  
429 subwatersheds at various scales in a time efficient manner. However, the results of Section 4 show that  
430 boundary differences exist between the watersheds delineated by our approach and those derived directly  
431 from rasters (i.e. ArcGIS, TauDEM, Arc Hydro Tools). The variations in watershed boundaries are a result  
432 of the datasets used to derive the NHD+ catchment boundaries and flow relationships, i.e. modified DEM  
433 and the WBD rasters used in combination with a watershed delineation algorithm designed to produce the

434 best agreement of available data (Johnston *et al.*, 2009). This method allows experts to modify remotely  
435 sensed terrain data to ensure that it is consistent with known field measurements, unlike traditional raster-  
436 based watershed delineation. However, the NHD+ dataset may contain processing errors such as those  
437 outlined in Figure 11. In situations such as this, a manual correction may have been made to the dataset  
438 to account for the actual hydrography of the surface (e.g. an obstruction to river flow), however it could  
439 also be a mistake. We must consider these watershed boundary differences inherent to the dataset used by  
440 our hierarchical algorithm, which in this case is the NHD+. If desired, a custom or alternate watershed  
441 boundary dataset can be used in place of the NHD+ for greater quality assurance. For example, this work  
442 uses the NHD+ version 1.0 dataset, however, a newer version of the dataset is now available that consists  
443 of the most accurate and up-to-date data. In fact, it appears that some of these boundary differences have  
444 been corrected in the NHD+ version 2. A significant advantage of our approach is its ability to easily adapt  
445 to newer, more accurate, datasets without having to process large datasets.

446 Overall, our technique consists of a light-weight software algorithm that is implemented in the Python  
447 programming language and mathematical graph theory to process watershed boundaries. NHD+ network  
448 relationships are stored in serialized graphs, while spatial data are stored in a PostgreSQL spatial database  
449 that leverages PostGIS functionality. However, this algorithm has also been adapted to leverage SQLite  
450 database storage. This versatility demonstrates the portability of this technique, and as a result, it may be  
451 a good candidate for remote hosting via web services or deployment in cloud environments. Future work will  
452 investigate how this technique can be deployed as a web service to provide on-demand watershed delineations  
453 by leveraging emerging cloud computing environments such as Microsoft Azure or Amazon Elastic Compute  
454 Cloud (EC2). A service such as this could then be used to retrieve, process, and summarize input data for  
455 models. In addition, this technique can be expanded upon to supply users with other NHD+ data products  
456 or attributes consisting of new or summarized data. This is particularly useful when preprocessing data to  
457 create model input files.

## 458 **6. Acknowledgments**

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460 laborative Research: CiC (SEA): Using the Cloud to Model and Manage Large Watershed Systems.”

## 461 **7. Software Availability**

462 The delineation software presented in this paper is available for download under the GNU General Public  
463 Licence V3 at <https://bitbucket.org/Castronova/hierarchical-watershed-delineation>.

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